# A Demonstration of the $\mathrm{AT}_{\mathrm{E}} \mathrm{X} 2_{\mathcal{E}}$ Class File for the Journal of Mathematical Study 

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#### Abstract

This paper describes the use of the $\mathrm{LA}_{\mathrm{E}} \mathrm{X} 2_{\varepsilon} \mathrm{jms}$. cls class file for setting papers for the Journal of Mathematical Study. AMS subject classifications: 52B10, 65D18, 68U05, 68U07 Chinese Library Classifications: O175.27


Key words: $\mathrm{ET}_{\mathrm{E}} \mathrm{X} 2 \varepsilon$

## 1 Introduction

This paper is described how to use the jms.cls class file for publication in the Journal of Mathematical Study. The jms.cls class file preserves much of the standard $\mathrm{LT}_{\mathrm{E}} \mathrm{X} 2_{\varepsilon}$ interface so that authors can easily convert their standard $\mathrm{LT}_{\mathrm{E}} 2_{\varepsilon}$ article style files to the jms style.

## 2 Preparation of Manuscript

The Title Page should contain the article title, authors' names and complete affiliations, and email addresses of all authors. The Abstract should provide a brief summary of the main findings of the paper.

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Illustrations in color in most cases can be accepted only if the authors defray the cost. At the Editor's discretion a limited number of color figures each year of special interest will be published at no cost to the author.

## 3 Mathematical Formulas (Examples)

In [1] it was claimed that there always exists a minimizer; however, the statement of Theorem 2.1 is incomplete. In this note we present the full statement, with a detailed proof.

The theorem stated in [1] holds as long as the number of electrons is below a certain critical value. The correct statement for the theorem in [1] is:

Theorem 3.1 (Existence of minimizers). Given $v \in C^{\infty}(\bar{\Omega})$, and $K_{W T} \in L_{l o c}^{2}\left(\mathbb{R}^{3}\right)$, consider the problem

$$
\begin{equation*}
\inf _{u \in \mathcal{B}} F[u], \tag{3.1}
\end{equation*}
$$

where $F$ and $\mathcal{B}$ are

$$
\begin{align*}
F[u]= & \frac{1}{2} \int_{\Omega}|\nabla u|^{2}-\frac{7 C_{T F} N^{2 / 3}}{25} \int_{\Omega} u^{10 / 3}+\frac{4 C_{T F} N^{2 / 3}}{5} \int_{\Omega}|u|^{5 / 3}\left(K_{W T} *|u|^{5 / 3}\right) \\
& +\frac{N}{2} \int_{\Omega} u^{2}\left(\frac{1}{|\mathbf{x}|} * u^{2}\right)-\frac{3}{4}\left(\frac{3 N}{\pi}\right)^{1 / 3} \int_{\Omega} u^{8 / 3} \\
& +\int_{\Omega} u^{2} \varepsilon\left(N u^{2}\right)+\int_{\Omega} v(\mathbf{x}) u^{2}(\mathbf{x}) d \mathbf{x}, \tag{3.2}
\end{align*}
$$

and

$$
\begin{equation*}
\mathcal{B}=\left\{u \in H_{0}^{1}(\Omega) \mid u \geq 0, \int_{\Omega} u^{2}=1\right\} . \tag{3.3}
\end{equation*}
$$

In (3.2), the set $\Omega$ is open and bounded, and star-shaped with respect to 0 ; $\varepsilon$ is defined as

$$
\varepsilon\left(N u^{2}\right)=\left\{\begin{array}{l}
\frac{\gamma}{1+\beta_{1} \sqrt{r_{s}}+\beta_{2} r_{s}}, \quad r_{s} \geq 1,  \tag{3.4}\\
A \ln \left(r_{s}\right)+B+C r_{s} \ln \left(r_{s}\right)+D r_{s}, \quad r_{s} \leq 1,
\end{array}\right.
$$

where $r_{s}=\left(4 \pi N u^{2} / 3\right)^{-\frac{1}{3}}$; the parameters used are $\gamma=-0.1423, \beta_{1}=1.0529, \beta_{2}=0.3334$, $A=0.0311, B=-0.048$, and $C=2.019151940622 \times 10^{-3}$ and $D=-1.163206637891 \times 10^{-2}$ are chosen so that $\varepsilon(r)$ and $\varepsilon^{\prime}(r)$ are continuous at $r=1$.

Then, there exists $N_{0}>0$ such that:

1. If $N<N_{0}$ then $\exists u^{*} \in \mathcal{B}$ such that

$$
\begin{equation*}
F\left[u^{*}\right]=\min _{u \in \mathcal{B}} F[u] . \tag{3.5}
\end{equation*}
$$

2. If $N>N_{0}$ then

$$
\begin{equation*}
\inf _{u \in \mathcal{B}} F[u]=-\infty \tag{3.6}
\end{equation*}
$$

Proof. The second part of the theorem was proved in $[2,3]$. We outline the proof here for completeness. Since $0 \in \Omega, \exists \delta_{0}>0$ such that $B\left(0, \delta_{0}\right) \subset \Omega$. Consider a compactly supported function $u_{0} \in C_{0}^{\infty}(B(0,1))$, such that

$$
\begin{equation*}
\int_{\mathbb{R}^{3}} u_{0}^{2}=1 \tag{3.7}
\end{equation*}
$$

and consider the rescaling

$$
\begin{equation*}
u_{\delta}(\mathbf{x})=\frac{1}{\delta^{3 / 2}} u_{0}\left(\frac{\mathbf{x}}{\delta}\right), \quad 0<\delta<\delta_{0} \tag{3.8}
\end{equation*}
$$

Then $u_{\delta} \in \mathcal{B}$, and

$$
\begin{equation*}
F\left[u_{\delta}\right]=\frac{1}{\delta^{2}}\left(\frac{1}{2} \int_{\Omega}\left|\nabla u_{0}\right|^{2}-\frac{7 C_{T F} N^{2 / 3}}{25} \int_{\Omega} u_{0}^{10 / 3}\right)+\mathcal{O}\left(\frac{1}{\delta}\right) \tag{3.9}
\end{equation*}
$$

Define

$$
\begin{equation*}
A_{0}=\inf _{u \in H_{0}^{1}(\Omega),\|u\|_{2}=1} \frac{\int_{\Omega}|\nabla u|^{2}}{\int_{\Omega} u^{10 / 3}}>0 \tag{3.10}
\end{equation*}
$$

Then if $A_{0} / 2<7 C_{T F} N^{2 / 3} / 25$, we can choose $u_{0}$ so that the leading term in (3.9) is negative, and when $\delta \rightarrow 0$, the desired result follows.

For the existence of minimizers, assume that $N$ is such that $A_{0} / 2>7 C_{T F} N^{2 / 3} / 25$. By Lemma 3.1, there exist $C>0, \delta>0$ such that

$$
\begin{align*}
& F[u] \geq \frac{1}{2} \int_{\Omega}|\nabla u|^{2}-\left(\frac{7 C_{T F} N^{2 / 3}}{25}+\delta\right) \int_{\Omega} u^{10 / 3}-C \\
\geq & \left(\frac{1}{2}-\frac{1}{A_{0}}\left(\frac{7 C_{T F} N^{2 / 3}}{25}+\delta\right)\right) \int_{\Omega}|\nabla u|^{2} \geq \tau \int_{\Omega}|\nabla u|^{2}-C, \tag{3.11}
\end{align*}
$$

where $\tau>0$. Therefore the functional is coercive, and the result follows from now from standard arguments in the Calculus of Variations, involving the Sobolev Embedding, and the Rellich-Kondrachov compactness theorem.

## 4 Header Information

The heading for any file using ata.cls is like this;
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\begin\{document\} }

\title\{Make the Title in Title Case\}

\author[An Author et. ~al]\{First Author $\backslash$ affil\{1\}, Second Author $\backslash$ affil $\{2\} \backslash$ comma\corrauth
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\address\{\affilnum\{1\}\ Address for first and third authors <br>
\affilnum\{2\}\ Address for second author\}
\emails\{\{\tt ata@global-sci.org\} (A. ~Author), \{\tt second@author.email\} (S.~Author), \{\tt third@author.email\}
(T. ~Author) \}
\begin\{abstract\} }
Text here, no equation, no citation, no reference.
\end\{abstract\} }
\ams\{list here\}
\clc\{list here\}
\keywords\{list here\}
\maketitle

\section\{First Section\}

\end\{document\} }

## 5 Some Remarks

### 5.1 Mathematics

jms.cls makes the full functionality of $\mathcal{A}_{\mathcal{M}} S \mathrm{~T}_{\mathrm{E}} \mathrm{X}$ available. We encourage the use of the align, gather and multine environments for displayed mathematics.

### 5.2 Cross-referencing

The use of the ${ }^{2} T_{E} X$ cross-reference system for figures, tables, equations and citations is encouraged.

## Acknowledgments

The author would like to thank ....

## References

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